



OnLine Lecture 115: Introduction to Characteristic Impedance

- Why this topic is important
 - ✓ Characteristic impedance is the most important topic in signal integrity
 - ✓ It is also the most confusing
 - ✓ There is a simple way of thinking about it that eliminates the confusion
 - ✓ A good understanding of characteristic impedance will train your intuition to help you be a much better designer
- Level
 - ✓ Introduction
- Recommended prerequisites:
 - ✓ none



Outline

- ✓ What is a transmission line
- ✓ What is impedance
- ✓ The instantaneous impedance a signal sees
- ✓ Characteristic impedance and instantaneous impedance
- ✓ Calculating characteristic impedance
- ✓ The impedance of a transmission line
- ✓ Return current in a transmission line

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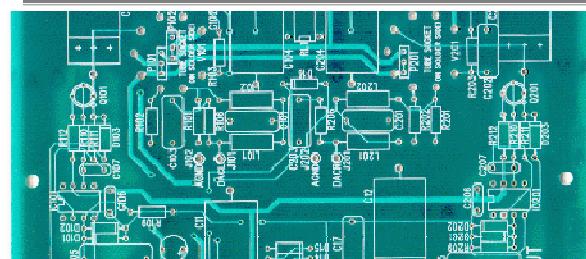
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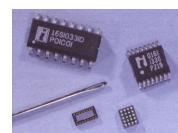
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What's a Transmission Line?



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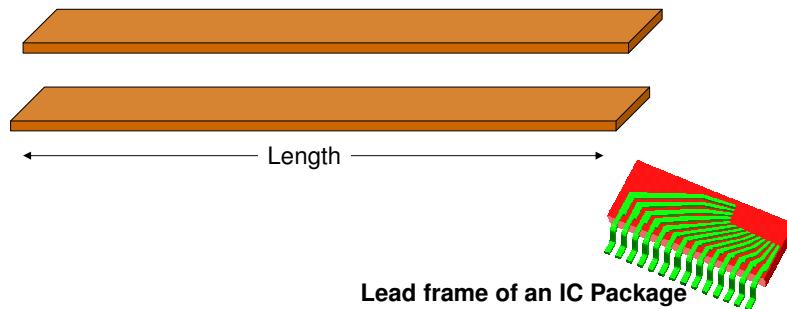
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The Simplest Model of a Transmission Line



A "-1" order model:
Any two conductors with length



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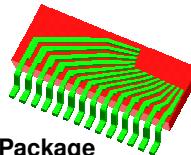
Classifying Transmission Lines by the Geometry of the Conductors

1. Uniform or non uniform down the length

- ✓ Uniform transmission lines have the same cross section down their length



- ✓ Non uniform transmission lines a changing cross section down their length



Lead frame of an IC Package
(pick any two leads)

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Classifying Transmission Lines by the Geometry of the Conductors

2. Balanced

or

unbalanced



twisted pair



coplanar



coax



microstrip



embedded microstrip



stripline



asymmetric stripline

(how identical the two conductors are)

What's a signal?

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Labeling the Conductors

Signal path



Return path

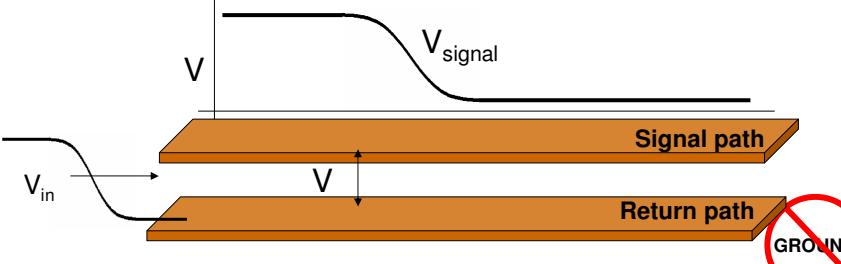


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Slide - 9a

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The Signal



V

V_{signal}

V_{in}

V

Signal path

Return path

GROUND

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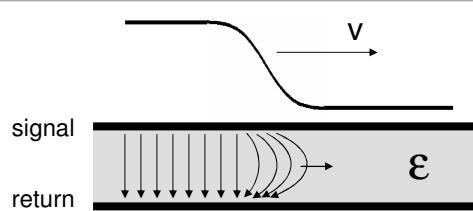
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Slide - 10a

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How fast does a signal move down a line?



V

signal

return

ϵ

in air: $v = 186,000$ miles per sec

$v = 12$ inches/nsec



$$V = \frac{12 \frac{\text{inches}}{\text{nsec}}}{\sqrt{4}} = \frac{12 \frac{\text{inches}}{\text{nsec}}}{2} = 6 \frac{\text{inches}}{\text{nsec}}$$

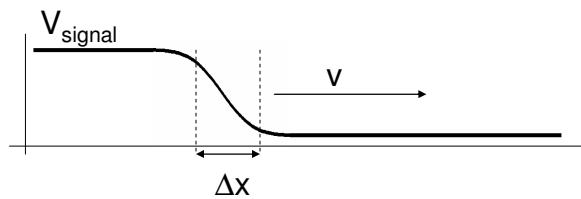
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Spatial Extent of the Leading Edge

RT = rise time



$$\Delta x = v \times RT$$

$$6 \text{ inches} = 6 \text{ inches/nsec} \times 1 \text{ nsec}$$

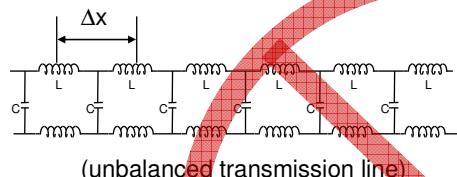
$$1.2 \text{ inch} = 6 \text{ inches/nsec} \times 0.2 \text{ nsec}$$

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First Order Model of a Transmission Line (Loss Less Model)



$$C = C_L \Delta x \quad \text{capacitance}$$

$$L = L_L \Delta x \quad \text{inductance}$$

The circuit analysis result:

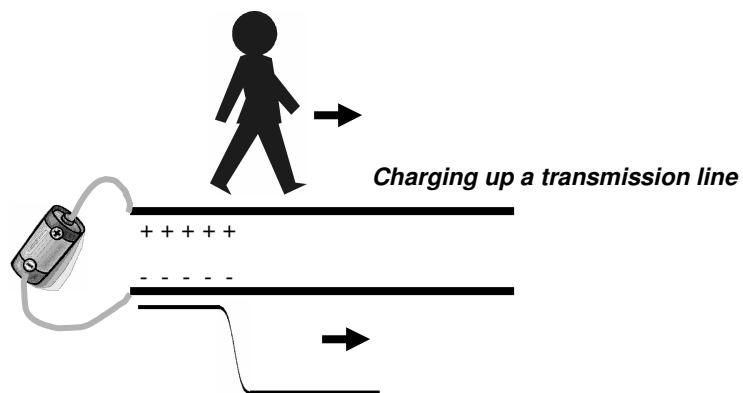
$$Z_0 = \sqrt{\frac{L_L}{C_L}} \quad TD = \sqrt{L_{\text{total}} C_{\text{total}}} \quad \tau = \frac{1}{\sqrt{L_L C_L}}$$

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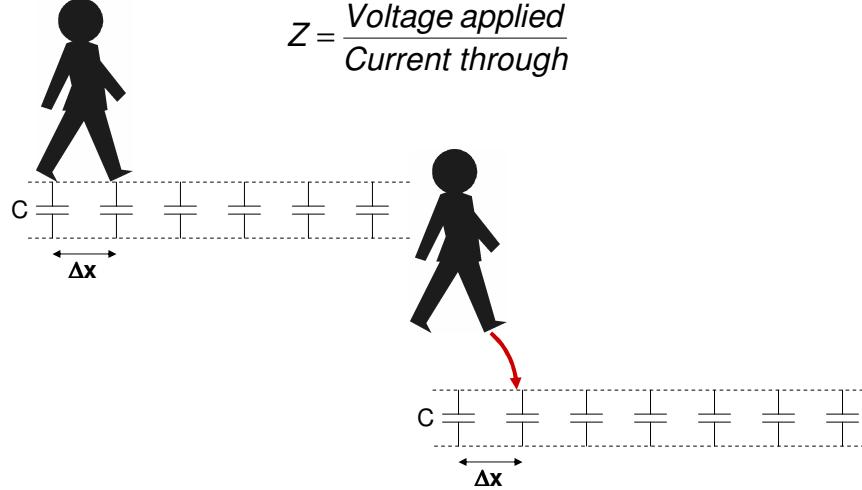
“...be the signal”



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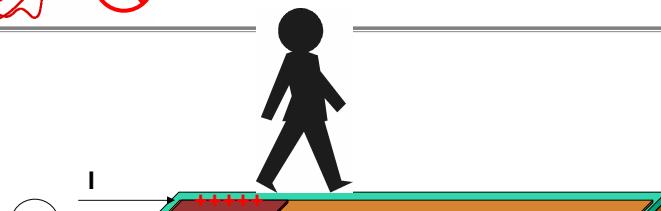
Building a simple model

$$Z = \frac{\text{Voltage applied}}{\text{Current through}}$$

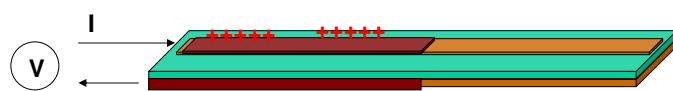


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A Propagating Signal



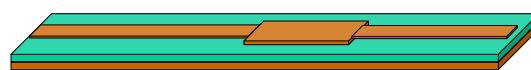
Charged line
after 1 nsec



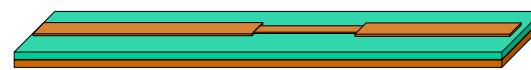
Charged line after 2 nsec

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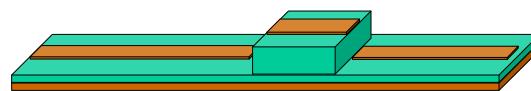
Geometry, Current and Impedance



Line width increases, impedance decreases



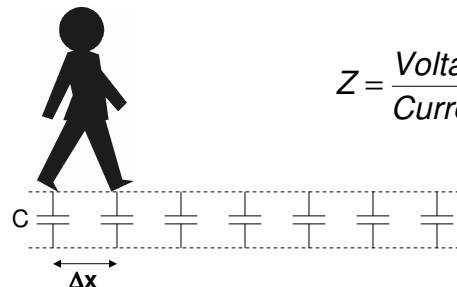
Line width decreases, impedance increases



Dielectric thickness increases, impedance, increases

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Instantaneous Impedance The Signal Sees

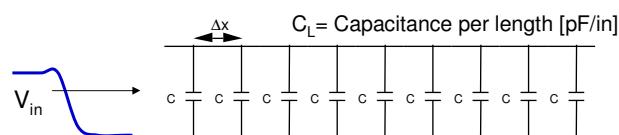


$$Z = \frac{\text{Voltage applied}}{\text{Current through}}$$

instantaneous impedance of the transmission line

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0th Order Model of Transmission Line



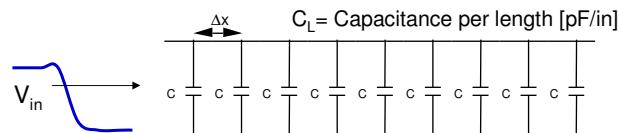
$$C = C_L \Delta x$$

$$\Delta Q = CV, \quad \text{every } \Delta t = \frac{\Delta x}{V}$$

What is the current into the line?

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Current Into Transmission Line



$$C = C_L \Delta x$$

$$\Delta Q = CV, \\ \text{every } \Delta t = \frac{\Delta x}{V}$$

I, V definition of
Transmission Line: $I = \frac{\Delta Q}{\Delta t} = \frac{V C_L \Delta x V}{\Delta x} = V C_L V$

What's the impedance?

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Instantaneous Impedance of a Transmission Line

$$I = V C_L V$$

$$Z = \frac{V}{I} = \frac{V}{V C_L V} = \frac{1}{V C_L}$$

Features of the impedance:

- looks like a resistor
- dependant on intrinsic properties
- independent of length

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Characteristic Impedance

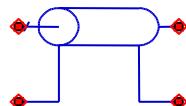
$$Z_0 = \frac{1}{\sqrt{C_L}}$$

- an intrinsic property of a transmission line
- independent of length
- is the instantaneous impedance a signal will see when propagating down a uniform section
- also called the “surge impedance” or “wave impedance”

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The Ideal, Lossless Transmission Line Model

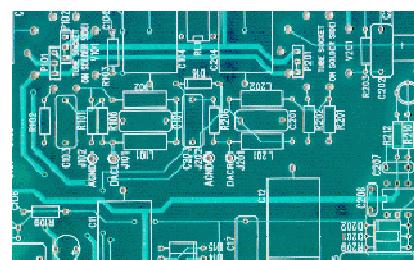
A “transmission line” is the name we use to refer to the an ideal electrical circuit element



a new, fundamental, ideal circuit element: T

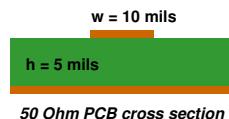
- Characteristic impedance, Z_0 ,
- Time delay: TD

A “transmission line” is also the name we use to refer to a real, physical interconnect



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Characteristic Impedance and Capacitance per Length



50 Ohm PCB cross section

increase h

capacitance per length decreases, the characteristic impedance increases

increase w

the capacitance per length increases, characteristic impedance decreases



$$Z_0 \sim \frac{1}{C_L}$$

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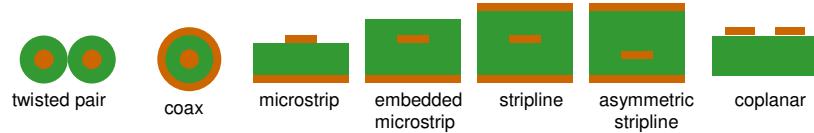
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Controlled Impedance

- Z_0 is constant down the length
- uniform capacitance per length: geometry and materials
- uniform velocity: materials
- any value Z_0 can be controlled impedance

Controlled impedance structures



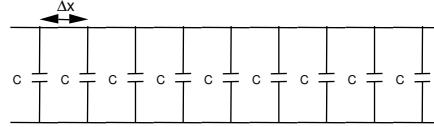
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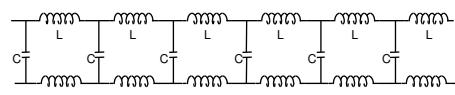
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What About the Inductance of the Line?

- Physical model:
 - ✓ capacitance per length
 - ✓ physical distance
 - ✓ finite propagation speed



- Electrical model:
 - capacitance per length
 - physical distance
 - Inductance per length



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Calculating Characteristic Impedance

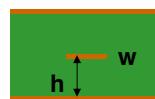
- Separating Myths from Reality: (OnLineLecture 000)
- Rules of Thumb (OnLineLecture 180)
- Approximations and 2D field solvers (OnLineLecture 130)
- Capacitance and inductance (OnLineLecture 120)

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Calculating Characteristic Impedance: Rules of Thumb



Microstrip:
50 Ohm line in FR4 has $w:h = 2:1$



Stripline:
50 Ohm line in FR4 has $w:h = 1:1$

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Calculating Characteristic Impedance: Approximations



$$Z_0 = \frac{87}{\sqrt{(\epsilon_r + 1.41)}} \ln\left(7.5 \frac{h}{w}\right)$$



$$Z_0 = \frac{60}{\sqrt{\epsilon_r}} \ln\left(2.35 \frac{b}{w}\right) \Omega$$



$$Z_0 = \frac{80}{\sqrt{\epsilon_r}} \ln\left(4.75 \frac{h1}{w}\right) \left(1 - \frac{h1}{4h2}\right)$$

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Accurate, Easy to Use 2D Field Solvers (absolute accuracy < 1%)

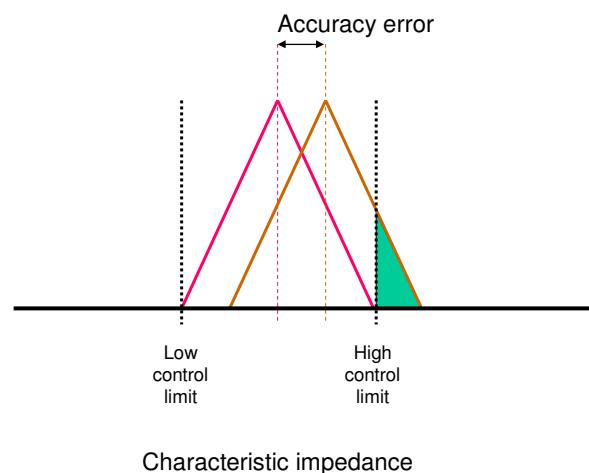
- Polar Instruments
 - ✓ Simplest to use
 - ✓ Dozens of pre-defined cross sections
 - ✓ No cross talk
- Hyperlynx
 - ✓ Simple
 - ✓ Impedance matrix elements
 - ✓ Integrated IBIS based simulator
- Ansoft SI 2D Extractor
 - ✓ Parameterizing
 - ✓ Mixed dielectrics
 - ✓ Arbitrary cross sections
 - ✓ Current distribution
 - ✓ Frequency dependent effects

Use a 2D field solver if:

1. Assured accuracy better than 20% is important
2. Etch back, solder mask or trace thickness are important
3. Mixed dielectrics are used
4. Cross talk is important

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Why High Accuracy Can Save Money



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Simplest to use 2D field solver

Polar Embedded Microstrip 1B1A www.polarinstruments.com

<i>H1</i>	<i>Er1</i>	<i>H2</i>	<i>Er2</i>	<i>W1</i>	<i>W2</i>	<i>T1</i>	<i>Calc Type</i>	<i>Z₀</i>
6	4.2	1	4.2	10	10	0.7	<i>Z₀</i>	51.1
6	4.2	2	4.2	10	10	0.7	<i>Z₀</i>	49.8
6	4.2	3	4.2	10	10	0.7	<i>Z₀</i>	49.0
6	4.2	4	4.2	10	10	0.7	<i>Z₀</i>	48.4
6	4.2	5	4.2	10	10	0.7	<i>Z₀</i>	48.0
6	4.2	6	4.2	10	10	0.7	<i>Z₀</i>	47.6
6	4.2	7	4.2	10	10	0.7	<i>Z₀</i>	47.3
6	4.2	8	4.2	10	10	0.7	<i>Z₀</i>	47.1
6	4.2	9	4.2	10	10	0.7	<i>Z₀</i>	46.9
6	4.2	10	4.2	10	10	0.7	<i>Z₀</i>	46.7
6	4.2	11	4.2	10	10	0.7	<i>Z₀</i>	46.6
6	4.2	12	4.2	10	10	0.7	<i>Z₀</i>	46.5
6	4.2	13	4.2	10	10	0.7	<i>Z₀</i>	46.4
6	4.2	14	4.2	10	10	0.7	<i>Z₀</i>	46.3
6	4.2	15	4.2	10	10	0.7	<i>Z₀</i>	46.3
6	4.2	16	4.2	10	10	0.7	<i>Z₀</i>	46.2
6	4.2	17	4.2	10	10	0.7	<i>Z₀</i>	46.1
6	4.2	18	4.2	10	10	0.7	<i>Z₀</i>	46.1
6	4.2	19	4.2	10	10	0.7	<i>Z₀</i>	46.1
6	4.2	20	4.2	10	10	0.7	<i>Z₀</i>	46.0
6	4.2	21	4.2	10	10	0.7	<i>Z₀</i>	46.0
6	4.2	22	4.2	10	10	0.7	<i>Z₀</i>	46.0
6	4.2	23	4.2	10	10	0.7	<i>Z₀</i>	45.9
6	4.2	24	4.2	10	10	0.7	<i>Z₀</i>	45.9
6	4.2	25	4.2	10	10	0.7	<i>Z₀</i>	45.9
6	4.2	26	4.2	10	10	0.7	<i>Z₀</i>	45.9
6	4.2	27	4.2	10	10	0.7	<i>Z₀</i>	45.8

Embedded Microstrip 1B1A

www.polarinstruments.com

Height (H2)

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Impedance of Controlled Impedance Transmission Lines

Famous Characteristic Impedances:

RG58	52 Ω
RG174	50 Ω
RG59	75 Ω
RG62	93 Ω
TV Antenna	300 Ω
Cable TV	75 Ω
Twisted pairs	100-120 Ω

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What's Special About 50Ω ?

1. Became international standard for instrumentation as radar proliferated.
2. Matches with most test and measurement equipment
3. Can be manufactured easily with circuit board technology.
4. Is a reasonable match to IC drivers.
5. Optimum value for high speed digital systems trades off between:
 - power dissipation with parallel termination
 - delay adders with capacitive loads
 - cross talk for reasonable spacing
 - manufacturability (total board thickness)
 - interfacing with test equipment and peripherals
 - "sweet spot" is 40Ω - 80Ω

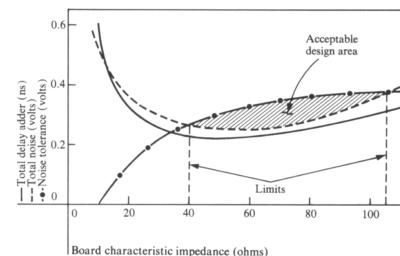
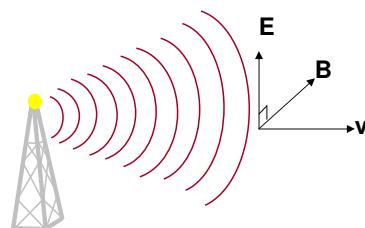


Figure 12 Design space for characteristic impedance.

"Electrical Design of a High Speed Computer Package", Evan Davidson, IBM J. of R&D, vol 26(3) May 1982, p. 349

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Characteristic Impedance of Free Space

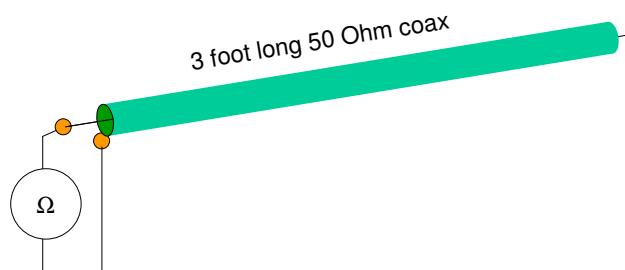


$$Z = \sqrt{\frac{B}{E}} = \sqrt{\frac{\mu_0}{\epsilon_0}} = \sqrt{\frac{4\pi 10^{-7} H/m}{8.85 \times 10^{-12} F/m}} = 376.8 \text{ Ohms}$$

Characteristic impedance of Free Space ~ 377 Ohms

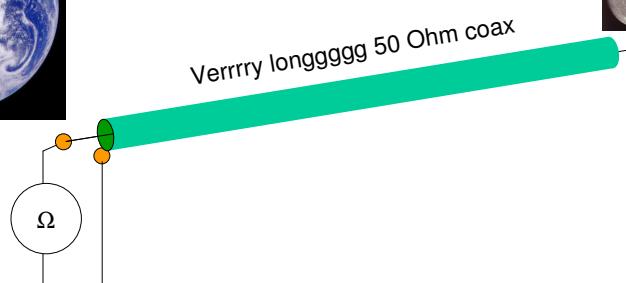
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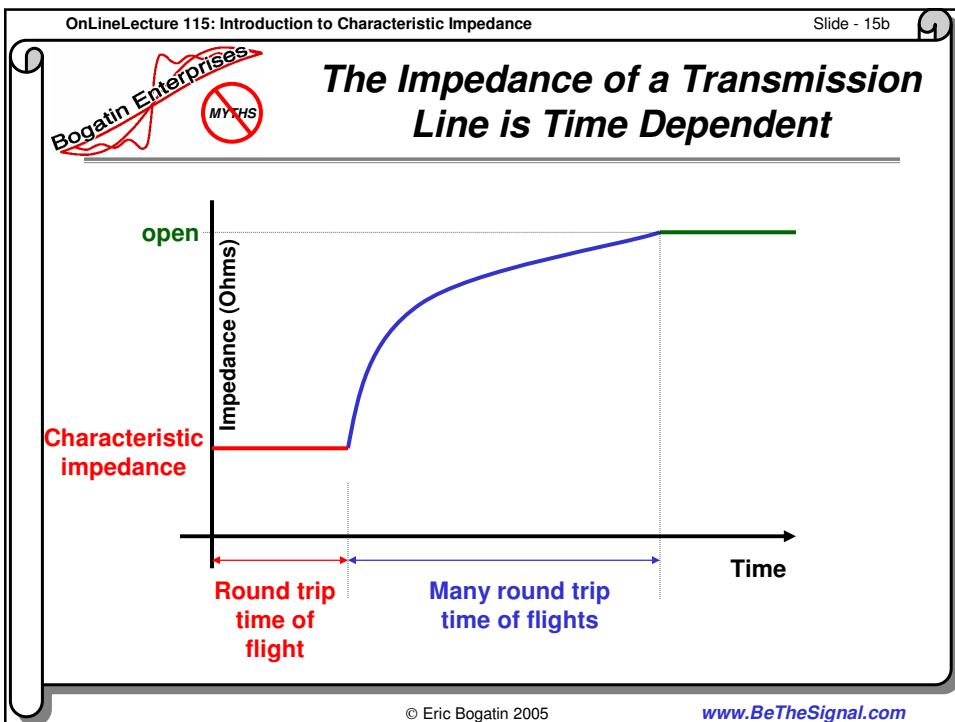
What Is the Measured Impedance of a 50 Ohm Cable?



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What Does it Mean to Have a 50 Ohm Line?





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Slide - 16b

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An important Distinction

- **THE** impedance of the transmission line (the input impedance) - may be time dependent
- The **instantaneous** impedance of the transmission line
- The **Characteristic** impedance of the transmission line

Just referring to "...the impedance" may be a bit ambiguous

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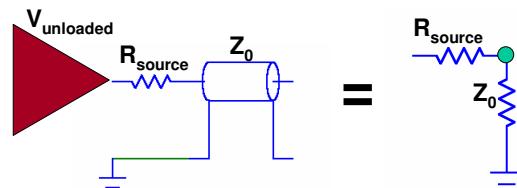
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The Input Impedance of the Transmission Line



If rise time < 2 x TD, what impedance does driver see during transition?

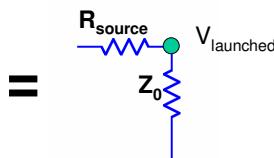
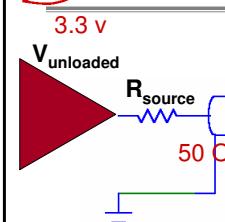


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Voltage Launched into the Line



$$V_{launched} = V_{unloaded} \frac{Z_0}{R_{source} + Z_0}$$

R_{source}	$V_{launched}$
20 Ohms	1.2 v
10 Ohms	2.75 v
5 Ohms	3.0 v
2 Ohms	3.17 v

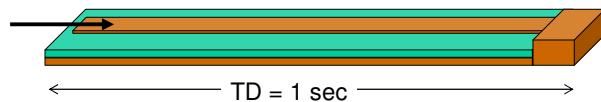
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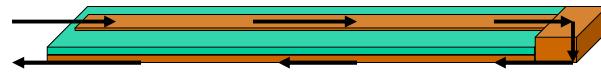
Return Path in T Lines

Current into signal line



When does the return current return?

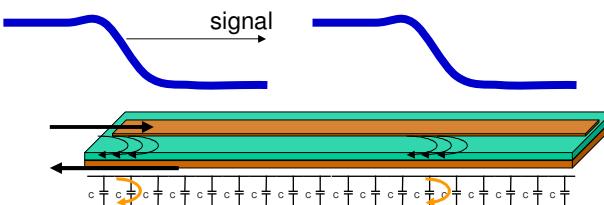
For DC currents:



For RF currents? When does current come out return path?

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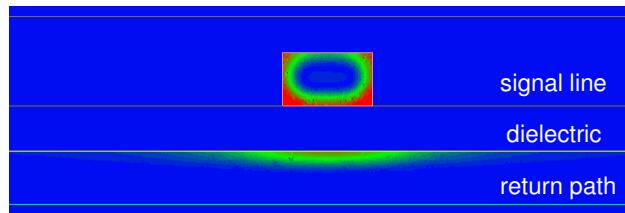
Return Current Paths in Transmission Lines



To control impedance, manage the return path as carefully as the signal path

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Current Distribution in a Microstrip



Current density
at 500 MHz

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Let's Review

- What's a transmission line?
 - ✓ Any two conductors with length
- What is the impedance of a transmission line?
 - ✓ The ratio of the voltage to the current for a signal propagating down the line
- What is characteristic impedance?
 - ✓ An intrinsic property of uniform cross section transmission lines that is equal to the instantaneous impedance the signal would see as it propagates
- What happens to the characteristic impedance of a microstrip if the line width is increased?
 - ✓ The capacitance goes up so the characteristic impedance would go down
- When a signal is launched into a transmission line, when does the return current come out?
 - ✓ At exactly the same time the current goes into the signal line, The current returns through the capacitance between the signal and return paths

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The End



Thanks for listening!

射 频 和 天 线 设 计 培 训 课 程 推 荐

易迪拓培训(www.edatop.com)由数名来自于研发第一线的资深工程师发起成立，致力并专注于微波、射频、天线设计研发人才的培养；我们于 2006 年整合合并微波 EDA 网(www.mweda.com)，现已发展成为国内最大的微波射频和天线设计人才培养基地，成功推出多套微波射频以及天线设计经典培训课程和 ADS、HFSS 等专业软件使用培训课程，广受客户好评；并先后与人民邮电出版社、电子工业出版社合作出版了多本专业图书，帮助数万名工程师提升了专业技术能力。客户遍布中兴通讯、研通高频、埃威航电、国人通信等多家国内知名公司，以及台湾工业技术研究院、永业科技、全一电子等多家台湾地区企业。

易迪拓培训课程列表：<http://www.edatop.com/peixun/rfe/129.html>



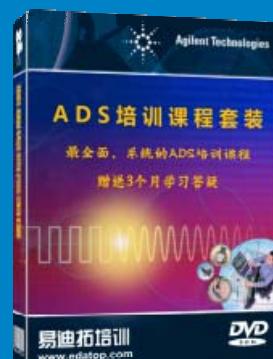
射频工程师养成培训课程套装

该套装精选了射频专业基础培训课程、射频仿真设计培训课程和射频电路测量培训课程三个类别共 30 门视频培训课程和 3 本图书教材；旨在引领学员全面学习一个射频工程师需要熟悉、理解和掌握的专业知识和研发设计能力。通过套装的学习，能够让学员完全达到和胜任一个合格的射频工程师的要求…

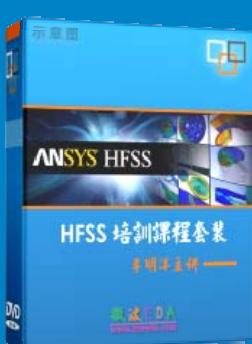
课程网址：<http://www.edatop.com/peixun/rfe/110.html>

ADS 学习培训课程套装

该套装是迄今国内最全面、最权威的 ADS 培训教程，共包含 10 门 ADS 学习培训课程。课程是由具有多年 ADS 使用经验的微波射频与通信系统设计领域资深专家讲解，并多结合设计实例，由浅入深、详细而又全面地讲解了 ADS 在微波射频电路设计、通信系统设计和电磁仿真设计方面的内容。能让您在最短的时间内学会使用 ADS，迅速提升个人技术能力，把 ADS 真正应用到实际研发工作中去，成为 ADS 设计专家…



课程网址：<http://www.edatop.com/peixun/ads/13.html>



HFSS 学习培训课程套装

该套课程套装包含了本站全部 HFSS 培训课程，是迄今国内最全面、最专业的 HFSS 培训教程套装，可以帮助您从零开始，全面深入学习 HFSS 的各项功能和在多个方面的工程应用。购买套装，更可超值赠送 3 个月免费学习答疑，随时解答您学习过程中遇到的棘手问题，让您的 HFSS 学习更加轻松顺畅…

课程网址：<http://www.edatop.com/peixun/hfss/11.html>

CST 学习培训课程套装

该培训套装由易迪拓培训联合微波 EDA 网共同推出, 是最全面、系统、专业的 CST 微波工作室培训课程套装, 所有课程都由经验丰富的专家授课, 视频教学, 可以帮助您从零开始, 全面系统地学习 CST 微波工作的各项功能及其在微波射频、天线设计等领域的设计应用。且购买该套装, 还可超值赠送 3 个月免费学习答疑…



课程网址: <http://www.edatop.com/peixun/cst/24.html>



HFSS 天线设计培训课程套装

套装包含 6 门视频课程和 1 本图书, 课程从基础讲起, 内容由浅入深, 理论介绍和实际操作讲解相结合, 全面系统的讲解了 HFSS 天线设计的全过程。是国内最全面、最专业的 HFSS 天线设计课程, 可以帮助您快速学习掌握如何使用 HFSS 设计天线, 让天线设计不再难…

课程网址: <http://www.edatop.com/peixun/hfss/122.html>

13.56MHz NFC/RFID 线圈天线设计培训课程套装

套装包含 4 门视频培训课程, 培训将 13.56MHz 线圈天线设计原理和仿真设计实践相结合, 全面系统地讲解了 13.56MHz 线圈天线的工作原理、设计方法、设计考量以及使用 HFSS 和 CST 仿真分析线圈天线的具体操作, 同时还介绍了 13.56MHz 线圈天线匹配电路的设计和调试。通过该套课程的学习, 可以帮助您快速学习掌握 13.56MHz 线圈天线及其匹配电路的原理、设计和调试…



详情浏览: <http://www.edatop.com/peixun/antenna/116.html>

我们的课程优势:

- ※ 成立于 2004 年, 10 多年丰富的行业经验,
- ※ 一直致力并专注于微波射频和天线设计工程师的培养, 更了解该行业对人才的要求
- ※ 经验丰富的一线资深工程师讲授, 结合实际工程案例, 直观、实用、易学

联系我们:

- ※ 易迪拓培训官网: <http://www.edatop.com>
- ※ 微波 EDA 网: <http://www.mweda.com>
- ※ 官方淘宝店: <http://shop36920890.taobao.com>